

Angles

Supplementary Angles
add to make 180°

Linear Pair
add to 180° and share a side

Complementary Angles
add to make 90°

Adjacent Angles are next to one another

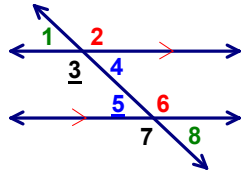
Vertical Angles are across and equal

Acute Angles are less than 90°

Right Angles are equal to 90°

Obtuse Angles are greater than 90° and less than 180°

Parallel Lines crossed by a Transversal



Alternate Interior Angles are equal Ex: $\angle 4 = \angle 5$

Alternate Exterior Angles are equal Ex: $\angle 1 = \angle 8$

Same Sided Interior Angles Add to 180° Ex: $\angle 3 + \angle 5 = 180^\circ$

Corresponding Angles are equal Ex: $\angle 2 = \angle 6$

Triangles

Classifying By Side Length:

Scalene: no sides the same

Isosceles: 2 sides the same

Equilateral: All sides the same

Classifying By Largest Angle³

Acute: less than 90°

Right: equal to 90°

Obtuse: greater than 90°

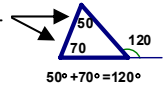
The Altitude can be inside, on or outside a triangle.



Interior Angles Sum to 180° in every triangle



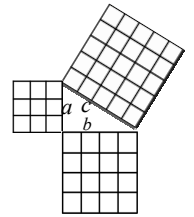
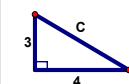
An Exterior Angle equals the sum of the two remote interior angles.



Pythagorean Theorem

$$a^2 + b^2 = c^2$$

Ex: Find c



$$3^2 + 4^2 = c^2$$

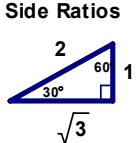
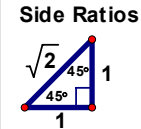
$$25 = c^2$$

$$5 = c$$

Special Right Triangles

45° 45° 90°

30° 60° 90°

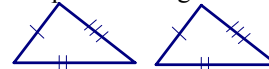


Lines and Planes

Term	Notation or Definition	Example
Line	\leftrightarrow AB	
Ray	\rightarrow AB	
Segment	\overline{AB}	
Collinear	Points on the same line	
Perpendicular	$AB \perp CD$	
Parallel	$WX \parallel YZ$	
Skew	AB and CD never hit And are not parallel	
Perpendicular Bisector	\overrightarrow{BD} divides segment AC in half and is perpendicular	
Plane	Plane z is a flat surface extending in all directions	
Coplanar	Points A, B and C are coplanar (on the same plane)	

Proving Two Triangles Congruent

SSS: 3 pairs of congruent sides



SAS: 2 pairs of congruent sides and one equal angle between



AAS: 2 pairs of congruent angles and one pair of congruent sides

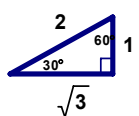
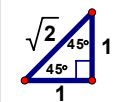


ASA: 2 pairs of congruent angles and 1 pair of congruent sides between



Side Ratios

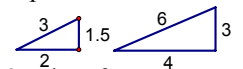
Side Ratios



Proving Two Triangles Similar

Sides must be in the same ratio and angles must be equal.

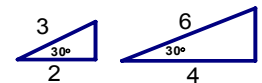
SSS: 3 pairs of similar sides



AA: 2 pairs of congruent angles



SAS: 2 pairs of similar sides & 1 pair of equal angles between

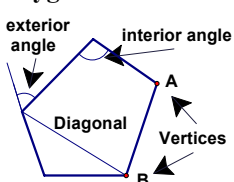


Polygons

Polygon: two-dimensional closed figure made of straight line segments connected end to end (& don't cross)



Polygon Parts:

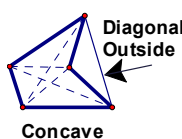


Convex Polygons: all diagonals are inside the shape



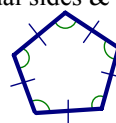
Convex

Concave Polygon: at least one diagonal is outside the shape



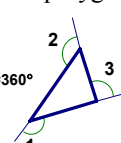
Concave

Regular Polygons have equal sides & angles



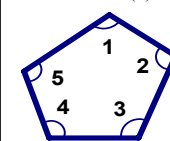
Sum of Exterior Angles in all polygons

$$\angle 1 + \angle 2 + \angle 3 = 360^\circ$$



Sum of Interior Angles = $(\# \text{ of sides} - 2) \cdot 180^\circ$

Ex: Sum the 5 angles below: $(5 \text{ sides} - 2) \cdot 180^\circ = (3) \cdot 180^\circ = 540^\circ$



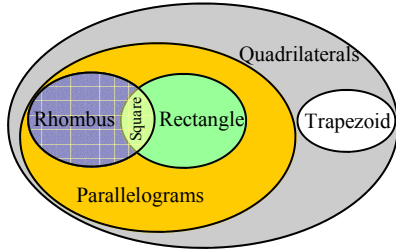
$$\angle 1 + \angle 2 + \angle 3 + \angle 4 + \angle 5 = 540$$

Quadrilateral	4 Sides
Pentagon	5 Sides
Hexagon	6 Sides
Heptagon	7 Sides
Octagon	8 Sides
Nonagon	9 Sides
Decagon	10 Sides
N-gon	N Sides

Quadrilaterals

Relationship Between Quadrilaterals

Ex: A Rectangle is a Parallelogram and a Quadrilateral but not a Trapezoid.



Quadrilateral 4 sided polygon



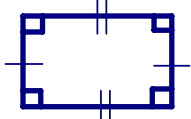
Trapezoids Quadrilateral with just 1 pair of parallel sides.



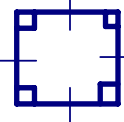
Isosceles Trapezoid also has 2 equal sides. (the non parallel sides)



Rectangle all angles are equal: 90°



Square all angles and all sides equal



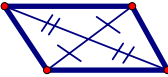
Parallelogram: 2 pairs of parallel sides



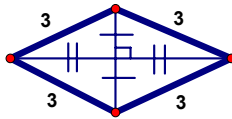
Opposite sides are also equal in length



Diagonals bisect one another



Rhombus all sides are equal & diagonals are perpendicular bisectors



Circles

Diameter: \overline{CD} goes across the circle through the center

Radius: \overline{OE} goes from the center to the outside of the circle

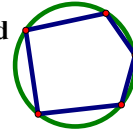
Chord: \overline{AB} connects 2 points on the circle

Secant: \overleftrightarrow{AB} intersects the circle in 2 points

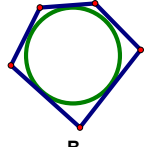
Tangent: \overleftrightarrow{EF} touches at 1 point and is perpendicular to the radius.

Concentric Circles have the same center

Polygon Inscribed in a circle



Polygon Circumscribed about a circle



ARCS

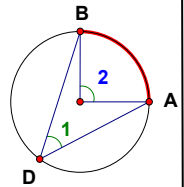
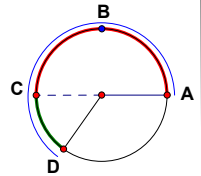
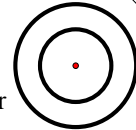
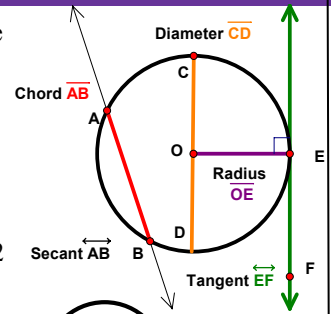
Semicircle: \overline{ABC} is half the circumference

Major Arc: \overline{ACD} is greater than 180°

Minor Arc: \overline{CD} is less than 180°

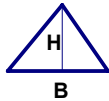
Central Angle: $\angle 2$ has a vertex at the center and is the same as arc \overline{AB}

Inscribed Angle: $\angle 1$ is half intercepted arc \overline{AB}



Area

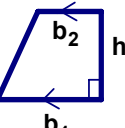
Triangle: $A = \frac{1}{2} B \cdot H$



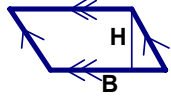
Circle: $A = \pi r^2$



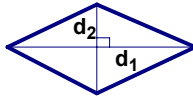
Trapezoid: $A = \frac{1}{2} (b_1 + b_2) h$



Parallelogram: $A = B \cdot H$

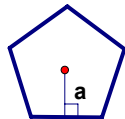


Rhombus: $A = \frac{1}{2} (d_1 \cdot d_2)$



Regular Polygon: $A = \frac{1}{2} a \cdot P$

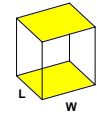
a=apothem P=perimeter



Volume

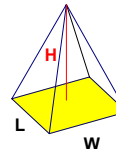
Prism: $V = (\text{area of base}) \cdot (\text{vertical height})$

For Rectangular base: $L \cdot W \cdot H$



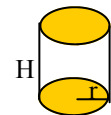
Pyramid: $V = \frac{1}{3} (\text{area of base}) \cdot (\text{vertical height})$

For rectangular base: $\frac{1}{3} L \cdot W \cdot H$



Cylinder: $V = [r^2 H]$

$V = (\text{area of base}) \cdot (\text{vertical height})$

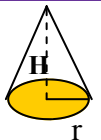


Sphere:

$V = \frac{4}{3} \pi r^3$ $\text{Area} = 4\pi r^2$



Cone: $V = \frac{1}{3} [r^2 H]$



Midpoint & Distance

Midpoint Formula: $\left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2} \right)$

Ex: Find the midpoint of (2,1) and (10,7)

$$\left(\frac{2+10}{2}, \frac{1+7}{2} \right) = \left(\frac{12}{2}, \frac{8}{2} \right) = (6, 4)$$

Distance Formula:

$$\sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

Ex: Find the distance from (1,2) to (4,6)

$$\begin{aligned} &= \sqrt{(4 - 1)^2 + (6 - 2)^2} \\ &= \sqrt{(3)^2 + (4)^2} \\ &= \sqrt{9 + 16} = \sqrt{25} = 5 \end{aligned}$$